

zero: (a) the gas moves up along the vertical line, (b) it moves down along the vertical line, (c) it moves to anywhere in region 1, and (d) it moves to anywhere in region 2.

3 For a temperature increase of ΔT_1 , a certain amount of an ideal gas requires 30 J when heated at constant volume and 50 J when heated at constant pressure. How much work is done by the gas in the second situation?

4 The dot in Fig. 19-15b represents the initial state of a gas, and the isotherm through the dot divides the p - V diagram into regions 1 and 2. For the following processes, determine whether the change ΔE_{int} in the internal energy of the gas is positive, negative, or zero: (a) the gas moves up along the isotherm, (b) it moves down along the isotherm, (c) it moves to anywhere in region 1, and (d) it moves to anywhere in region 2.

5 An ideal diatomic gas, with molecular rotation but not oscillation, loses energy as heat Q . Is the resulting decrease in the internal energy of the gas greater if the loss occurs in a constant-volume process or in a constant-pressure process?

6 The dot in Fig. 19-15c represents the initial state of a gas, and the adiabat through the dot divides the p - V diagram into regions 1 and 2. For the following processes, determine whether the corresponding heat Q is positive, negative, or zero: (a) the gas moves up along the adiabat, (b) it moves down along the adiabat, (c) it moves to anywhere in region 1, and (d) it moves to anywhere in region 2.

7 A certain amount of energy is to be transferred as heat to 1 mol of a monatomic gas (a) at constant pressure and (b) at

constant volume, and to 1 mol of a diatomic gas (c) at constant pressure and (d) at constant volume. Figure 19-16 shows four paths from an initial point to four final points on a p - V diagram. Which path goes with which process? (e) Are the molecules of the diatomic gas rotating?

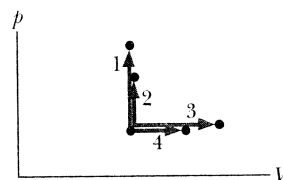


Fig. 19-16 Question 7.

8 Does the temperature of an ideal gas increase, decrease, or stay the same during (a) an isothermal expansion, (b) an expansion at constant pressure, (c) an adiabatic expansion, and (d) an increase in pressure at constant volume?

9 (a) Rank the four paths of Fig. 19-14 according to the work done by the gas, greatest first. (b) Rank paths 1, 2, and 3 according to the change in the internal energy of the gas, most positive first and most negative last.

10 In the p - V diagram of Fig. 19-17, the gas does 5 J of work when taken along isotherm ab and 4 J when taken along adiabat bc . What is the change in the internal energy of the gas when it is taken along the straight path from a to c ?

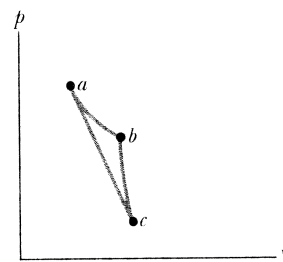


Fig. 19-17 Question 10.

Problems

- SSM Solution is in the Student Solutions Manual.
 WWW Solution is at <http://www.wiley.com/college/halliday>
 ILW Interactive LearningWare solution is at
<http://www.wiley.com/college/halliday>
 • • • Number of dots indicates level of problem difficulty.

sec. 19-2 Avogadro's Number

- 1 Find the mass in kilograms of 7.50×10^{24} atoms of arsenic, which has a molar mass of 74.9 g/mol.
 •2 Gold has a molar mass of 197 g/mol. (a) How many moles of gold are in a 2.50 g sample of pure gold? (b) How many atoms are in the sample?

sec. 19-3 Ideal Gases

- 3 Compute (a) the number of moles and (b) the number of molecules in 1.00 cm^3 of an ideal gas at a pressure of 100 Pa and a temperature of 220 K.
 •4 The best laboratory vacuum has a pressure of about $1.00 \times 10^{-18} \text{ atm}$, or $1.01 \times 10^{-13} \text{ Pa}$. How many gas molecules are there per cubic centimeter in such a vacuum at 293 K?
 •5 Oxygen gas having a volume of 1000 cm^3 at 40.0°C and $1.01 \times 10^5 \text{ Pa}$ expands until its volume is 1500 cm^3 and its pressure is $1.06 \times 10^5 \text{ Pa}$. Find (a) the number of moles of oxygen present and (b) the final temperature of the sample. SSM

- 6 An automobile tire has a volume of $1.64 \times 10^{-2} \text{ m}^3$ and contains air at a gauge pressure (pressure above atmospheric pressure) of 165 kPa when the temperature is 0.00°C . What is the gauge pressure of the air in the tires when its temperature rises to 27.0°C and its volume increases to $1.67 \times 10^{-2} \text{ m}^3$? Assume atmospheric pressure is $1.01 \times 10^5 \text{ Pa}$.
 •7 A quantity of ideal gas at 10.0°C and 100 kPa occupies a volume of 2.50 m^3 . (a) How many moles of the gas are present? (b) If the pressure is now raised to 300 kPa and the temperature is raised to 30.0°C , how much volume does the gas occupy? Assume no leaks.
 •8 Suppose 1.80 mol of an ideal gas is taken from a volume of 3.00 m^3 to a volume of 1.50 m^3 via an isothermal compression at 30°C . (a) How much energy is transferred as heat during the compression, and (b) is the transfer to or from the gas?
 •9 A container encloses 2 mol of an ideal gas that has molar mass M_1 and 0.5 mol of a second ideal gas that has molar mass $M_2 = 3M_1$. What fraction of the total pressure on the container wall is attributable to the second gas? (The kinetic theory explanation of pressure leads to the experimentally discovered law of partial pressures for a mixture of gases that do not react chemically: *The total pressure exerted by the mixture is equal to the sum of the pressures that the several gases would exert separately if each were to occupy the vessel alone.*)
 ••10 Suppose 0.825 mol of an ideal gas undergoes an isothermal expansion as energy is added to it as heat Q . If Fig.

19-18 shows the final volume V_f versus Q , what is the gas temperature?

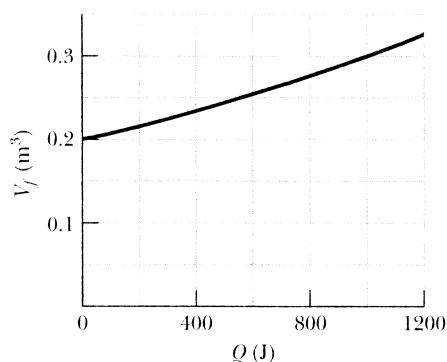


Fig. 19-18 Problem 10.

••11 In the temperature range 310 K to 330 K, the pressure p of a certain nonideal gas is related to volume V and temperature T by

$$p = (24.9 \text{ J/K}) \frac{T}{V} - (0.00662 \text{ J/K}^2) \frac{T^2}{V}.$$

How much work is done by the gas if its temperature is raised from 315 K to 325 K while the pressure is held constant?

••12 A sample of an ideal gas is taken through the cyclic process $abca$ shown in Fig. 19-19; at point a , $T = 200$ K. (a) How many moles of gas are in the sample? What are (b) the temperature of the gas at point b , (c) the temperature of the gas at point c , and (d) the net energy added to the gas as heat during the cycle?

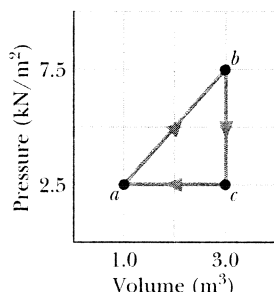


Fig. 19-19 Problem 12.

••13 Air that initially occupies 0.140 m^3 at a gauge pressure of 103.0 kPa is expanded isothermally to a pressure of 101.3 kPa and then cooled at constant pressure until it reaches its initial volume. Compute the work done by the air. (Gauge pressure is the difference between the actual pressure and atmospheric pressure.) *SSM ILW WWW*

•••14 An air bubble of volume 20 cm^3 is at the bottom of a lake 40 m deep, where the temperature is 4.0°C . The bubble rises to the surface, which is at a temperature of 20°C . Take the temperature of the bubble's air to be the same as that of the surrounding water. Just as the bubble reaches the surface, what is its volume?

•••15 Container A in Fig. 19-20 holds an ideal gas at a pressure of $5.0 \times 10^5 \text{ Pa}$ and a temperature of 300 K . It is connected by a thin tube (and a closed valve) to container B, with four times the volume of A. Container B holds the same ideal gas at a pressure of $1.0 \times 10^5 \text{ Pa}$ and a temperature of 400 K . The valve is opened to allow the pressures to equalize,

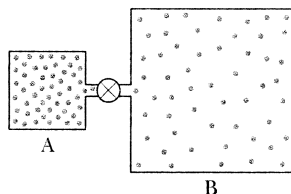


Fig. 19-20 Problem 15.

but the temperature of each container is maintained. What then is the pressure in the two containers? *ILW*

sec. 19-4 Pressure, Temperature, and RMS Speed

•16 Find the rms speed of argon atoms at 313 K . See Appendix F for the molar mass of argon atoms.

•17 The lowest possible temperature in outer space is 2.7 K . What is the rms speed of hydrogen molecules at this temperature? (The molar mass of hydrogen molecules (H_2) is given in Table 19-1.) *SSM*

•18 Calculate the rms speed of helium atoms at 1000 K . See Appendix F for the molar mass of helium atoms.

•19 (a) Compute the rms of a nitrogen molecule at 20.0°C . The molar mass of nitrogen molecules (N_2) is given in Table 19-1. At what temperatures will the rms speed be (b) half that value and (c) twice that value?

•20 The temperature and pressure in the Sun's atmosphere are $2.00 \times 10^6 \text{ K}$ and 0.0300 Pa . Calculate the rms speed of free electrons (mass $9.11 \times 10^{-31} \text{ kg}$) there, assuming they are an ideal gas.

••21 A beam of hydrogen molecules (H_2) is directed toward a wall, at an angle of 55° with the normal to the wall. Each molecule in the beam has a speed of 1.0 km/s and a mass of $3.3 \times 10^{-24} \text{ g}$. The beam strikes the wall over an area of 2.0 cm^2 , at the rate of 10^{23} molecules per second. What is the beam's pressure on the wall? *SSM*

••22 At 273 K and $1.00 \times 10^{-2} \text{ atm}$, the density of a gas is $1.24 \times 10^{-5} \text{ g/cm}^3$. (a) Find v_{rms} for the gas molecules. (b) Find the molar mass of the gas and (c) identify the gas. (*Hint:* The gas is listed in Table 19-1.)

sec. 19-5 Translational Kinetic Energy

•23 What is the average translational kinetic energy of nitrogen molecules at 1600 K ?

•24 Determine the average value of the translational kinetic energy of the molecules of an ideal gas at (a) 0.00°C and (b) 100°C . What is the translational kinetic energy per mole of an ideal gas at (c) 0.00°C and (d) 100°C ?

••25 Water standing in the open at 32.0°C evaporates because of the escape of some of the surface molecules. The heat of vaporization (539 cal/g) is approximately equal to ϵn , where ϵ is the average energy of the escaping molecules and n is the number of molecules per gram. (a) Find ϵ . (b) What is the ratio of ϵ to the average kinetic energy of H_2O molecules, assuming the latter is related to temperature in the same way as it is for gases?

sec. 19-6 Mean Free Path

•26 At what frequency would the wavelength of sound in air be equal to the mean free path of oxygen molecules at 1.0 atm pressure and 0.00°C ? Take the diameter of an oxygen molecule to be $3.0 \times 10^{-8} \text{ cm}$.

•27 The atmospheric density at an altitude of 2500 km is about 1 molecule/cm^3 . (a) Assuming the molecular diameter of $2.0 \times 10^{-8} \text{ cm}$, find the mean free path predicted by Eq. 19-25. (b) Explain whether the predicted value is meaningful. *SSM*

•28 The mean free path of nitrogen molecules at 0.0°C and 1.0 atm is $0.80 \times 10^{-5} \text{ cm}$. At this temperature and pressure

there are 2.7×10^{19} molecules/cm³. What is the molecular diameter?

••29 In a certain particle accelerator, protons travel around a circular path of diameter 23.0 m in an evacuated chamber, whose residual gas is at 295 K and 1.00×10^{-6} torr pressure. (a) Calculate the number of gas molecules per cubic centimeter at this pressure. (b) What is the mean free path of the gas molecules if the molecular diameter is 2.00×10^{-8} cm?

••30 At 20°C and 750 torr pressure, the mean free paths for argon gas (Ar) and nitrogen gas (N₂) are $\lambda_{\text{Ar}} = 9.9 \times 10^{-6}$ cm and $\lambda_{\text{N}_2} = 27.5 \times 10^{-6}$ cm. (a) Find the ratio of the diameter of an Ar atom to that of an N₂ molecule. What is the mean free path of argon at (b) 20°C and 150 torr, and (c) -40°C and 750 torr?

sec. 19-7 The Distribution of Molecular Speeds

•31 The speeds of 10 molecules are 2.0, 3.0, 4.0, . . . , 11 km/s. What are their (a) average speed and (b) rms speed? **SSM**

•32 The speeds of 22 particles are as follows (N_i represents the number of particles that have speed v_i):

N_i	2	4	6	8	2
v_i (cm/s)	1.0	2.0	3.0	4.0	5.0

What are (a) v_{avg} , (b) v_{rms} , and (c) v_p ?

•33 Ten particles are moving with the following speeds: four at 200 m/s, two at 500 m/s, and four at 600 m/s. Calculate their (a) average and (b) rms speeds. (c) Is $v_{\text{rms}} > v_{\text{avg}}$?

••34 Figure 19-21 gives the probability distribution for nitrogen gas. What are the (a) gas temperature and (b) rms speed of the molecules?

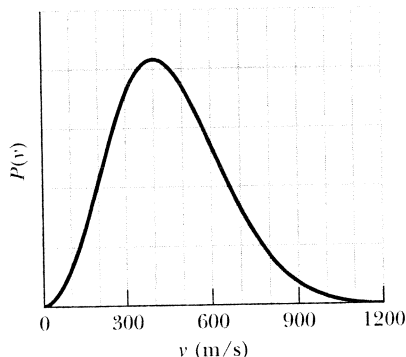


Fig. 19-21 Problem 34.

••35 At what temperature does the rms speed of (a) H₂ (molecular hydrogen) and (b) O₂ (molecular oxygen) equal the escape speed from Earth (Table 13-2)? At what temperature does the rms speed of (c) H₂ and (d) O₂ equal the escape speed from the Moon (where the gravitational acceleration at the surface has magnitude 0.16g)? Considering the answers to parts (a) and (b), should there be much (e) hydrogen and (f) oxygen high in Earth's upper atmosphere, where the temperature is about 1000 K?

••36 It is found that the most probable speed of molecules in a gas when it has (uniform) temperature T_2 is the same as the rms speed of the molecules in this gas when it has (uniform) temperature T_1 . Calculate T_2/T_1 .

••37 A hydrogen molecule (diameter 1.0×10^{-8} cm), traveling at the rms speed, escapes from a 4000 K furnace into a chamber containing cold argon atoms (diameter 3.0×10^{-8} cm) at a density of 4.0×10^{19} atoms/cm³. (a) What is the speed of the hydrogen molecule? (b) If it collides with an argon atom, what is the closest their centers can be, considering each as spherical? (c) What is the initial number of collisions per second experienced by the hydrogen molecule? (*Hint:* Assume that the argon atoms are stationary. Then the mean free path of the hydrogen molecule is given by Eq. 19-26 and not Eq. 19-25.)

••38 Two containers are at the same temperature. The first contains gas with pressure p_1 , molecular mass m_1 , and rms speed $v_{\text{rms}1}$. The second contains gas with pressure $2.0p_1$, molecular mass m_2 , and average speed $v_{\text{avg}2} = 2.0v_{\text{rms}1}$. Find the mass ratio m_1/m_2 .

••39 Figure 19-22 shows a hypothetical speed distribution for a sample of N gas particles (note that $P(v) = 0$ for speed $v > 2v_0$). What are the values of (a) av_0 , (b) v_{avg}/v_0 , and (c) v_{rms}/v_0 ? (d) What fraction of the particles has a speed between $1.5v_0$ and $2.0v_0$? **SSM WWW**

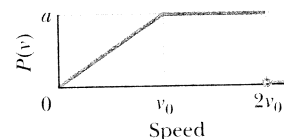


Fig. 19-22 Problem 39.

sec. 19-8 The Molar Specific Heats of an Ideal Gas

•40 What is the internal energy of 1.0 mol of an ideal monatomic gas at 273 K?

••41 The temperature of 2.00 mol of an ideal monatomic gas is raised 15.0 K at constant volume. What are (a) the work W done by the gas, (b) the energy transferred as heat Q , (c) the change ΔE_{int} in the internal energy of the gas, and (d) the change ΔK in the average kinetic energy per atom?

••42 Under constant pressure, the temperature of 2.00 mol of an ideal monatomic gas is raised 15.0 K. What are (a) the work W done by the gas, (b) the energy transferred as heat Q , (c) the change ΔE_{int} in the internal energy of the gas, and (d) the change ΔK in the average kinetic energy per atom?

••43 A container holds a mixture of three nonreacting gases: 2.40 mol of gas 1 with $C_{v1} = 12.0$ J/mol · K, 1.50 mol of gas 2 with $C_{v2} = 12.8$ J/mol · K, and 3.20 mol of gas 3 with $C_{v3} = 20.0$ J/mol · K. What is C_v of the mixture? **SSM**

••44 When 20.9 J was added as heat to a particular ideal gas, the volume of the gas changed from 50.0 cm³ to 100 cm³ while the pressure remained at 1.00 atm. (a) By how much did the internal energy of the gas change? If the quantity of gas present was 2.00×10^{-3} mol, find (b) C_p and (c) C_v .

••45 The mass of a gas molecule can be computed from its specific heat at constant volume c_v . (Note that this is not C_v .) Take $c_v = 0.075$ cal/g · °C for argon and calculate (a) the mass of an argon atom and (b) the molar mass of argon. **ILW**

••46 One mole of an ideal diatomic gas goes from a to c along the diagonal path in Fig. 19-23. During the transition,

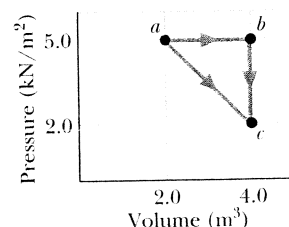


Fig. 19-23 Problem 46.

(a) what is the change in internal energy of the gas, and (b) how much energy is added to the gas as heat? (c) How much heat is required if the gas goes from *a* to *c* along the indirect path *abc*?

***47 In an industrial process the volume of 25.0 mol of a monatomic ideal gas is reduced at a uniform rate from 0.616 m³ to 0.308 m³ in 2.00 h while its temperature is increased at a uniform rate from 27.0°C to 450°C. Throughout the process, the gas passes through thermodynamic equilibrium states. What are (a) the cumulative work done on the gas, (b) the cumulative energy absorbed by the gas as heat, and (c) the molar specific heat for the process? (*Hint:* To evaluate the integral for the work, you might use

$$\int \frac{a + bx}{A + Bx} dx = \frac{bx}{B} + \frac{aB - bA}{B^2} \ln(A + Bx),$$

an indefinite integral.) Suppose the process is replaced with a two-step process that reaches the same final state. In step 1, the gas volume is reduced at constant temperature, and in step 2 the temperature is increased at constant volume. For this process, what are (d) the cumulative work done on the gas, (e) the cumulative energy absorbed by the gas as heat, and (f) the molar specific heat for the process?

sec. 19-9 Degrees of Freedom and Molar Specific Heats

•48 We give 70 J as heat to a diatomic gas, which then expands at constant pressure. The gas molecules rotate but do not oscillate. By how much does the internal energy of the gas increase?

•49 When 1.0 mol of oxygen (O₂) gas is heated at constant pressure starting at 0°C, how much energy must be added to the gas as heat to double its volume? (The molecules rotate but do not oscillate.) *ILW*

••50 Suppose 12.0 g of oxygen (O₂) gas is heated at constant atmospheric pressure from 25.0°C to 125°C. (a) How many moles of oxygen are present? (See Table 19-1 for the molar mass.) (b) How much energy is transferred to the oxygen as heat? (The molecules rotate but do not oscillate.) (c) What fraction of the heat is used to raise the internal energy of the oxygen?

••51 Suppose 4.00 mol of an ideal diatomic gas, with molecular rotation but not oscillation, experienced a temperature increase of 60.0 K under constant-pressure conditions. What are (a) the energy transferred as heat *Q*, (b) the change ΔE_{int} in internal energy of the gas, (c) the work *W* done by the gas, and (d) the change ΔK in the total translational kinetic energy of the gas? *SSM WWW*

sec. 19-11 The Adiabatic Expansion of an Ideal Gas

•52 We know that for an adiabatic process $pV^\gamma = \text{constant}$. Evaluate “a constant” for an adiabatic process involving exactly 2.0 mol of an ideal gas passing through the state having exactly $p = 1.0$ atm and $T = 300$ K. Assume a diatomic gas whose molecules rotate but do not oscillate.

•53 A certain gas occupies a volume of 4.3 L at a pressure of 1.2 atm and a temperature of 310 K. It is compressed adiabatically to a volume of 0.76 L. Determine (a) the final pressure and (b) the final temperature, assuming the gas to be an ideal gas for which $\gamma = 1.4$.

•54 Suppose 1.00 L of a gas with $\gamma = 1.30$, initially at 273 K and 1.00 atm, is suddenly compressed adiabatically to half its

initial volume. Find its final (a) pressure and (b) temperature. (c) If the gas is then cooled to 273 K at constant pressure, what is its final volume?

••55 Figure 19-24 shows two paths that may be taken by a gas from an initial point *i* to a final point *f*. Path 1 consists of an isothermal expansion (work is 50 J in magnitude), an adiabatic expansion (work is 40 J in magnitude), an isothermal compression (work is 30 J in magnitude), and then an adiabatic compression (work is 25 J in magnitude). What is the change in the internal energy of the gas if the gas goes from point *i* to point *f* along path 2?

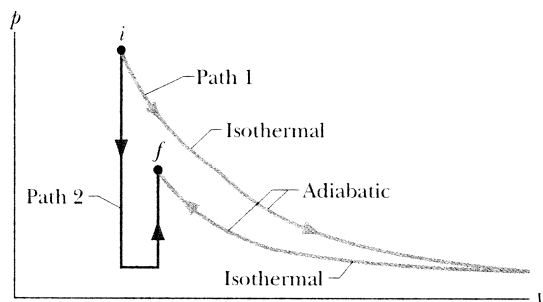


Fig. 19-24 Problem 55.

••56 The volume of an ideal gas is adiabatically reduced from 200 L to 74.3 L. The initial pressure and temperature are 1.00 atm and 300 K. The final pressure is 4.00 atm. (a) Is the gas monatomic, diatomic, or polyatomic? (b) What is the final temperature? (c) How many moles are in the gas?

••57 A gas is to be expanded from initial state *i* to final state *f* along either path 1 or path 2 on a *p-V* diagram. Path 1 consists of three steps: an isothermal expansion (work is 40 J in magnitude), an adiabatic expansion (work is 20 J in magnitude), and another isothermal expansion (work is 30 J in magnitude). Path 2 consists of two steps: a pressure reduction at constant volume and an expansion at constant pressure. What is the change in the internal energy of the gas along path 2?

••58 (a) An ideal gas initially at pressure p_0 undergoes a free expansion until its volume is 3.00 times its initial volume. What then is the ratio of its pressure to p_0 ? (b) The gas is next slowly and adiabatically compressed back to its original volume. The pressure after compression is $(3.00)^{1/3}p_0$. Is the gas monatomic, diatomic, or polyatomic? (c) What is the ratio of the average kinetic energy per molecule in this final state to that in the initial state?

••59 Figure 19-25 shows a cycle undergone by 1.00 mol of an ideal monatomic gas. For 1 → 2, what are (a) heat *Q*, (b) the change in internal energy ΔE_{int} , and (c) the work done *W*? For 2 → 3, what are (d) *Q*, (e) ΔE_{int} , and (f) *W*? For 3 → 1, what are (g) *Q*, (h) ΔE_{int} , and (i) *W*? For the full cycle, what are (j) *Q*, (k) ΔE_{int} , and (l) *W*? The initial pressure at point 1 is 1.00 atm ($= 1.013 \times 10^5$ Pa). What are the (m) volume and (n) pressure at point 2 and the (o) volume and (p) pressure at point 3? *SSM*

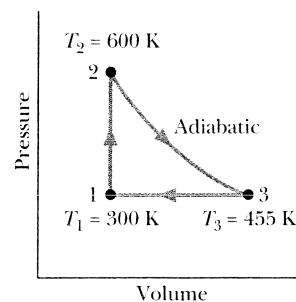


Fig. 19-25 Problem 59.

Additional Problems

60 An ideal gas is taken through a complete cycle in three steps: adiabatic expansion with work equal to 125 J, isothermal contraction at 325 K, and increase in pressure at constant volume. (a) Draw a p - V diagram for the three steps. (b) How much energy is transferred as heat in step 3, and (c) is it transferred *to* or *from* the gas?

61 (a) What is the volume occupied by 1.00 mol of an ideal gas at standard conditions—that is, 1.00 atm ($= 1.01 \times 10^5$ Pa) and 273 K? (b) Show that the number of molecules per cubic centimeter (the *Loschmidt number*) at standard conditions is 2.69×10^{19} .

62 In an interstellar gas cloud at 50.0 K, the pressure is 1.00×10^{-8} Pa. Assuming that the molecular diameters of the gases in the cloud are all 20.0 nm, what is their mean free path?

63 The envelope and basket of a hot-air balloon have a combined weight of 2.45 kN, and the envelope has a capacity (volume) of 2.18×10^3 m³. When it is fully inflated, what should be the temperature of the enclosed air to give the balloon a *lifting capacity* (force) of 2.67 kN (in addition to the balloon's weight)? Assume that the surrounding air, at 20.0°C, has a weight per unit volume of 11.9 N/m³ and a molecular mass of 0.028 kg/mole, and is at a pressure of 1.0 atm.

64 A container holds a gas of molecular hydrogen (H_2) at 250 K. What are (a) the most probable speed v_p of the molecules and (b) the maximum value P_{\max} of the probability distribution function $P(v)$? (c) With a graphing calculator or computer math package, determine what percentage of the molecules have speeds between $0.500v_p$ and $1.50v_p$. The temperature is then increased to 500 K. What are (d) the most probable speed v_p of the molecules and (e) the maximum value P_{\max} of the probability distribution function $P(v)$? Did (f) v_p and (g) P_{\max} increase, decrease, or remain the same because of the temperature increase?

65 The temperature of 3.00 mol of a gas with $C_V = 6.00$ cal/mol·K is to be raised 50.0 K. If the process is at *constant volume*, what are (a) the energy transferred as heat Q , (b) the work W done by the gas, (c) the change ΔE_{int} in internal energy of the gas, and (d) the change ΔK in the total translational kinetic energy? If the process is at *constant pressure*, what are (e) Q , (f) W , (g) ΔE_{int} , and (h) ΔK ? If the process is *adiabatic*, what are (i) Q , (j) W , (k) ΔE_{int} , and (l) ΔK ?

66 An ideal gas is suddenly allowed to expand freely so that the ratio of its new volume V_1 to its initial volume V_0 is $V_1/V_0 = 5.00$. The gas is then adiabatically compressed back to its initial volume V_0 , leaving it with a pressure p_2 that is $(5.00)^{0.40}$ times its initial pressure p_0 . (a) Is the gas monatomic, diatomic with no rotation of the molecules, diatomic with rotating molecules, or polyatomic? What is the ratio of the final value of the average kinetic energy per molecule to the initial value (b) after the free expansion and (c) after the adiabatic compression?

67 For adiabatic processes in an ideal gas, show that (a) the bulk modulus is given by

$$B = -V \frac{dp}{dV} = \gamma p,$$

and therefore (b) the speed of sound in the gas is

$$v_s = \sqrt{\frac{\gamma p}{\rho}} = \sqrt{\frac{\gamma RT}{M}}.$$

See Eqs. 17-2 and 17-3.

68 Air at 0.000°C and 1.00 atm pressure has a density of 1.29×10^{-3} g/cm³, and the speed of sound in air is 331 m/s at that temperature. Use those data and the results of Problem 67 to compute the ratio γ of the molar specific heats of air.

69 The molar mass of iodine is 127 g/mol. A standing wave in a tube filled with iodine gas at 400 K has nodes that are 6.77 cm apart when the frequency is 1400 Hz. (a) What is γ for iodine gas? (b) Is iodine gas monatomic or diatomic? (*Hint:* See Problem 67.)

70 Oxygen (O_2) gas at 273 K and 1.0 atm is confined to a cubical container 10 cm on a side. Calculate $\Delta U_g/K_{\text{avg}}$, where ΔU_g is the change in the gravitational potential energy of an oxygen molecule falling the height of the box and K_{avg} is the molecule's average translational kinetic energy.

71 The temperature of 2.00 mol of an ideal monatomic gas is raised 15.0 K in an adiabatic process. What are (a) the work W done by the gas, (b) the energy transferred as heat Q , (c) the change ΔE_{int} in internal energy of the gas, and (d) the change ΔK in the average kinetic energy per atom?

72 An ideal diatomic gas, with rotation but no oscillation, undergoes an adiabatic expansion. Its initial pressure and volume are 1.20 atm and 0.200 m³. Its final pressure is 2.40 atm. How much work is done by the gas?

73 During a compression at a constant pressure of 250 Pa, the volume of an ideal gas decreases from 0.80 m³ to 0.20 m³. The initial temperature is 360 K, and the gas loses 210 J as heat. What are (a) the change in the internal energy of the gas and (b) the final temperature of the gas?

74 An ideal gas consists of 1.50 mol of diatomic molecules that rotate but do not oscillate. The molecular diameter is 250 pm. The gas is expanded at a constant pressure of 1.50×10^5 Pa, with a transfer of 200 J as heat. What is the change in the mean free path of the molecules?

75 At what frequency do molecules collide in oxygen gas (O_2) at temperature 400 K and pressure 2.00 atm? Assume that the molecular diameter is 290 pm and that the gas is ideal.

76 An ideal monatomic gas initially has a temperature of 330 K and a pressure of 6.00 atm. It is to expand from volume 500 cm³ to volume 1500 cm³. If the expansion is isothermal, what are (a) the final pressure and (b) the work done by the gas? If, instead, the expansion is adiabatic, what are (c) the final pressure and (d) the work done by the gas?

77 An ideal gas with 3.00 mol is initially in state 1 with pressure $p_1 = 20.0$ atm and volume $V_1 = 1500$ cm³. First it is taken to state 2 with pressure $p_2 = 1.50p_1$ and volume $V_2 = 2.00V_1$. Then it is taken to state 3 with pressure $p_3 = 2.00p_1$ and volume $V_3 = 0.500V_1$. What is the temperature of the gas in (a) state 1 and (b) state 2? (c) What is the net change in internal energy from state 1 to state 3?

78 An ideal gas undergoes an adiabatic compression from $p = 1.0$ atm, $V = 1.0 \times 10^6$ L, $T = 0.0^\circ\text{C}$ to $p = 1.0 \times 10^5$

atm, $V = 1.0 \times 10^3$ L. (a) Is the gas monatomic, diatomic, or polyatomic? (b) What is its final temperature? (c) How many moles of gas are present? What is the total translational kinetic energy per mole (d) before and (e) after the compression? (f) What is the ratio of the squares of the rms speeds before and after the compression?

79 A sample of ideal gas expands from an initial pressure and volume of 32 atm and 1.0 L to a final volume of 4.0 L. The initial temperature is 300 K. If the gas is monatomic and the expansion isothermal, what are the (a) final pressure p_f , (b) final temperature T_f , and (c) work W done by the gas? If the gas is monatomic and the expansion adiabatic, what are (d) p_f , (e) T_f , and (f) W ? If the gas is diatomic and the expansion adiabatic, what are (g) p_f , (h) T_f , and (i) W ?

80 An ideal gas, at initial temperature T_1 and initial volume 2.0 m^3 , is expanded adiabatically to a volume of 4.0 m^3 , then expanded isothermally to a volume of 10 m^3 , and then compressed adiabatically back to T_1 . What is its final volume?

81 Calculate the work done by an external agent during an isothermal compression of 1.00 mol of oxygen from a volume of 22.4 L at 0°C and 1.00 atm to a volume of 16.8 L.

82 A steel tank contains 300 g of ammonia gas (NH_3) at a pressure of 1.35×10^6 Pa and a temperature of 77°C . (a) What is the volume of the tank in liters? (b) Later the temperature is 22°C and the pressure is 8.7×10^5 Pa. How many grams of gas have leaked out of the tank?

83 The mass of a helium atom is 6.66×10^{-27} kg. Compute the specific heat at constant volume for (monatomic) helium gas (in $\text{kJ/kg} \cdot \text{K}$) from the molar specific heat C_V .

84 (a) What is the molar volume (volume per mole) of an ideal gas at standard conditions (0.00°C , 1.00 atm)? (b) Calculate the ratio of the rms speed of helium atoms to that of neon atoms under these conditions. (c) What is the mean free path of helium atoms under these conditions? Assume the atomic diameter d of helium to be 1.00×10^{-8} cm. (d) What is the mean free path of neon atoms under these conditions? Assume they have the same atomic diameter as helium. (e) Comment on the results of (c) and (d) in view of the fact that the helium atoms are traveling faster than the neon atoms.

85 Figure 19-26 shows a cycle consisting of five paths: AB is isothermal at 300 K, BC is adiabatic with work = 5.0 J, CD is at a constant pressure of 5 atm, DE is isothermal, and EA is adiabatic with a change in internal energy of 8.0 J. What is the change in internal energy of the gas along path CD ?

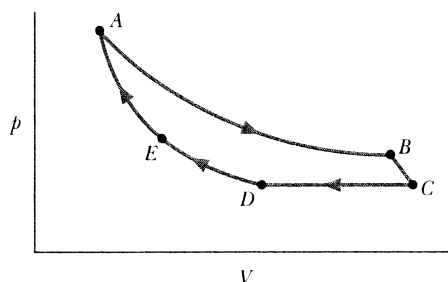


Fig. 19-26
Problem 85.

86 At what temperature do atoms of helium gas have the same rms speed as molecules of hydrogen gas at 20.0°C ? (The molar masses are given in Table 19-1.)

87 A quantity of an ideal monatomic gas consists of n moles initially at temperature T_1 . The pressure and volume are then slowly doubled in such a manner as to trace out a straight line on a p - V diagram. For this process, what are the ratios (a) W/nRT_1 , (b) $\Delta E_{\text{int}}/nRT_1$, and (c) Q/nRT_1 ? (d) If C is defined as the molar specific heat for the process, what is C/R ?

88 An ideal gas initially has a volume of 4.00 m^3 , a pressure of 5.67 Pa, and a temperature of -56.0°C . The gas is then expanded to 7.00 m^3 , leaving it with a temperature of 40.0°C . What then is the pressure?

89 Figure 19-27 shows a hypothetical speed distribution for particles of a certain gas: $P(v) = Cv^2$ for $0 < v \leq v_0$ and $P(v) = 0$ for $v > v_0$. Find (a) an expression for C in terms of v_0 , (b) the average speed of the particles, and (c) their rms speed.

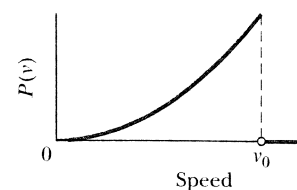


Fig. 19-27 Problem 89.

90 The temperature of 3.00 mol of an ideal diatomic gas is increased by 40.0°C without the pressure of the gas changing. The molecules in the gas rotate but do not oscillate. (a) How much energy is transferred to the gas as heat? (b) What is the change in the internal energy of the gas? (c) How much work is done by the gas? (d) By how much does the translational kinetic energy of the gas increase?

91 An ideal gas undergoes isothermal compression from an initial volume of 4.00 m^3 to a final volume of 3.00 m^3 . There is 3.50 mol of the gas, and its temperature is 10.0°C . (a) How much work is done by the gas? (b) How much energy is transferred as heat between the gas and its environment?

92 (a) What is the number of molecules per cubic meter in air at 20°C and at a pressure of 1.0 atm ($=1.01 \times 10^5$ Pa)? (b) What is the mass of 1.0 m^3 of this air? Assume that 75% of the molecules are nitrogen (N_2) and 25% are oxygen (O_2).

93 An ideal gas initially at 300 K is compressed at a constant pressure of 25 N/m^2 from a volume of 3.0 m^3 to a volume of 1.8 m^3 . In the process, 75 J is lost by the gas as heat. What are (a) the change in internal energy of the gas and (b) the final temperature of the gas?

94 Figure 19-28 represents an adiabatic compression of 2.0 mol of an ideal gas from 15 m^3 to 12 m^3 , followed by an isothermal compression at 300 K to a final volume of 3.0 m^3 . What is the total energy transferred as heat?

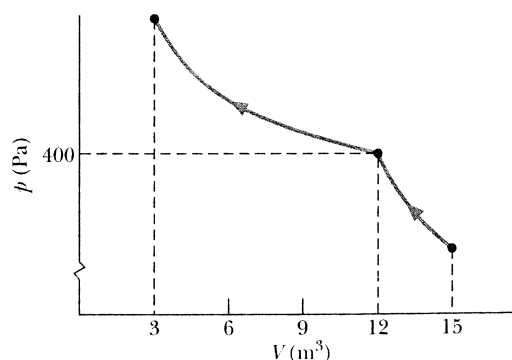


Fig. 19-28 Problem 94.